Table II. Dimer Orientations and Heats of Formation of WaterAcetaldehyde Dimers ${ }^{a, b}$

| $R_{\mathrm{OO},} \AA$ | $\theta_{1}, \mathrm{deg}$ | $\chi_{1}, \mathrm{deg}$ | $\chi_{2}, \mathrm{deg}$ | $\Delta H_{\mathrm{F}}{ }^{\circ}$ <br> $\mathrm{kcal} / \mathrm{mol}$ |
| :---: | :---: | :---: | :---: | :---: |
| 2.85 | 119 | 0 | 0 | -88.3 |
| 2.65 | 119 | 0 | 0 | -83.8 |
| 2.45 | 119 | 0 | 0 | -76.6 |
| 2.86 | 123 | 0 | 180 | -87.8 |
| $\infty$ |  |  |  | -97.2 |

${ }^{a}$ Heat of formation of water is $-53.6 \mathrm{kcal} / \mathrm{mol}$ and heat of formation of acetaldehyde is $-43.6 \mathrm{kcal} / \mathrm{mol}$. $\mathrm{R}_{\mathrm{OO}}$ is the distance between the oxygen atom of water and the carbonyl oxygen. $\theta$ is the angle between the internuclear line ( $x$ axis) and the principal axis of acetaldehyde. $\chi_{1}$ and $\chi_{2}$ measure the rotation of the molecules about their principal axes (see Figure 2).
author, we obtained a repulsion of 8.9 kcal which could not be reduced by varying the geometry (Table II). These results lead us to conclude that the MINDO/3 method is not suitable for the evaluation of hydrogen bonding and casts a serious doubt on the credibility of the numerous calculations that have been made with this method on intermolecular complexes.

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## On the Mechanism of the Cope Rearrangement

Sir:
Despite intensive work, ${ }^{1}$ the mechanism of the [3,3]-sigmatropic shift of 1,5 -hexadienes remains unclear. At issue is whether it is a concerted process via a single transition state with partial bonding between $C_{1}$ and $C_{6}$ and between $C_{3}$ and $\mathrm{C}_{4}$ or whether cyclohexane-1,4-diyl (a biradicaloid) is an intermediate.

The latter alternative, suggested by Grob ${ }^{2 a}$ and by Doering, ${ }^{2 b}$ is supported both theoretically by MINDO calculations ${ }^{3}$ and McIver's rules ${ }^{4}$ and experimentally by a constant multiplicative rate increase upon 2-phenyl and 2,5-diphenyl substitution. ${ }^{5}$ However, the experimental observations could equally well be due to a change in a single transition state toward a diyl-like species.


Unfortunately, the elegant stereochemical studies of Doering and Roth ${ }^{6}$ and of Hill ${ }^{7}$ are consistent with both alternatives; these results require a chair-like arrangement of six carbons in the lowest energy pathway. The single-stage concerted path should proceed suprafacially (or antarafacially) on both allylic moieties according to the orbital symmetry conservation principle, ${ }^{8}$ and secondary considerations favor the chair over the boat. ${ }^{8}$ On the other hand, the diyl is apparently generated in the thermal isomerization of bicyclo[2.2.0]hexanes ( BCH ) to 1,5 -hexadienes, and the stereochemistry observed is consistent with least-motion cleavage of a chair-like cyclohexanediyl. 9.10

We wish to point out that, if the cyclohexanediyl is involved in the cleavage of BCH, as experiment and MINDO calculations suggest, then it is not accessible in the 3,3 shift of 1,5 hexadiene by $12 \mathrm{kcal} / \mathrm{mol}$. Using Goldstein's values for the heats of formation and entropies of the relevant species at 250 ${ }^{\circ} \mathrm{C},{ }^{9 \mathrm{c}} \mathrm{BCH}$ is $18 \mathrm{kcal} / \mathrm{mol}$ less stable (in free energy) than 1,5-hexadiene. The transition state for BCH cleavage, which is that for cleavage of the diyl, is $53 \mathrm{kcal} / \mathrm{mol}$ above 1,5 -hexadiene. The low-energy 3,3 -shift transition state is only 41 $\mathrm{kcal} / \mathrm{mol}$ above 1,5-hexadiene.


The thermochemistry therefore indicates that the diyl, regardless of its stability, is insulated from the low-energy 3,3shift energy surface by a kinetic barrier $12 \mathrm{kcal} / \mathrm{mol}$ above the actual transition state, which, by elimination, is that for the single-stage concerted route.

Evidence that the diyl is involved in the BCH cleavage comes from the work of Goldstein who demonstrated that exo-endo isomerization of $2,3,5,6$-tetradeuterio-BCH occurs at the same rate as cleavage to 1,5 -hexadiene. ${ }^{10}$ This geometric isomerization would appear to involve central bond rupture to a boat diyl which flips through the chair diyl to the boat again. The cleavage presumably proceeds from the chair diyl as even the MINDO calculations suggest. ${ }^{3 \mathrm{a}}$

Just why the MINDO calculations lead to a prediction of inordinate stability for the diyl or why McIver's rules based

on transition state theory lead to the postulate of the diyl as an intermediate must be addressed by their proponents. It may be conceivable that a symmetrical, delocalized species is an intermediate in the 3,3 shift, but this would represent a unique situation not previously considered in hydrocarbon thermal isomerizations.

It should also be noted that MINDO calculations ${ }^{11}$ and McIver's rules ${ }^{12}$ predict an unsymmetrical transition state in the Diels-Alder reaction, but Thornton's multiplicative deuterium kinetic isotope effects in a retro-Diels-Alder reaction suggest a symmetrical transition state. ${ }^{13,14}$

Finally, the notion that substitution at various positions can alter the geometry of the transition state in any 3,3 shift is an important one which rationalizes not only the increase in rate of 2- and 2,5 -phenyl materials but the rate increases owing to substitution at $\mathrm{C}_{3}$ and $\mathrm{C}_{4}$. These transition-state changes are also reflected by secondary deuterium kinetic isotope effects. ${ }^{15.16}$

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(16) With good radical stabilizing substituents at $C_{2}$ and $C_{5}$ of 1,5-hexadiene, thermochemical estimates similar to those above suggest that a cyclo-hexane-1.4-diyl might be accessible in the 3.3 shift.

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## Variable Transition-State Structure in the Cope Rearrangement as Deduced from Secondary Deuterium Kinetic Isotope Effects

## Sir:

An accompanying communication demonstrates that the 3,3 shift in 1,5-hexadiene (the Cope rearrangement) does not proceed via cyclohexane-1,4-diyl, but by the only alternative yet proposed, namely, a concerted reaction via a single transition state in which there is partial bonding between $\mathrm{C}_{1}$ and $C_{6}$ and between $C_{3}$ and $C_{4} .{ }^{1}$ While the gross geometry of this transition state has been demonstrated by Doering and Roth and by Hill to be a "chair", 2 the question of the magnitude of

the partial bonds between the allylic moieties still must be resolved. While we cannot answer this question in an absolute sense, previous work with substituted materials, herein further elaborated with secondary deuterium kinetic isotope effects (KIE's), suggests a dramatic change in the magnitudes of these partial bonds as a function of substituents.

It is well known that good radical-stabilizing substituents not only on $\mathrm{C}_{3}$ and $\mathrm{C}_{4}$ but on $\mathrm{C}_{2}$ and $\mathrm{C}_{5}$ of 1,5 -hexadiene accelerate the rate of the 3,3 shift. ${ }^{4}$ In the|former case the rate response suggests that the transition state more resembles two allyl radicals, while in the latter case it more resembles cy-clohexane-1,4-diyl. Indeed, these two extremes represent, to a first approximation, the range of transition-state structures available to the 3,3 shift. ${ }^{4 \mathrm{~b}}$ These two extremes represent a range of weak to large coupling of two allyl radicals. A convenient representational device to depict this range of transi-tion-state structures is a More O'Ferrall-Jencks diagram ${ }^{5}$ whose structural axes are the $\mathrm{C}_{1}-\mathrm{C}_{6}$ and the $\mathrm{C}_{3}-\mathrm{C}_{4}$ bond orders. ${ }^{46,6}$ The free-energy coordinate might be represented by contours which are best not included for sake of clarity. However, the relative free energies of the extremes with respect to 1,5 -hexadiene, at $200^{\circ} \mathrm{C}$, can be guessed to a crude approximation from group additivities. ${ }^{7}$ It is also true that the transition-state free-energy for diyl cleavage is $53 \mathrm{kcal} / \mathrm{mol}$ above 1,5 -hexadiene; ${ }^{1}$ so a high-energy ridge surrounds the diyl but the exact location of the ridge is unknown.


Within the context of this diagram and discussions surrounding it, stabilization of either of the radical extremes should draw the transition-state structure toward the more stable alternative, ${ }^{5}$ and so secondary deuterium KIE's, which respond primarily to changes in force constants which to first approximation reflect bonding changes, ought to reveal these changes. ${ }^{8}$

The KIE's at $C_{4}$ and $C_{6}$ in the irreversible rearrangement of a 1,2-dialkyl-3,3-dicyano-1,5-hexadiene have been determined, and the normal KIE at $\mathrm{C}_{4}$ is three times the inverse KIE at $\mathrm{C}_{6},{ }^{9}$ In work described below the normal KIE at $\mathrm{C}_{3}$ and $\mathrm{C}_{4}$ in nearly unperturbed acyclic systems is roughly one half to two thirds that of the inverse KIE at $\mathrm{C}_{1}$ and $\mathrm{C}_{6}$, while in 2-phenyl-1,5-hexadiene the normal KIE at $\mathrm{C}_{3}$ and $\mathrm{C}_{4}$ is roughly one third of the inverse KIE at $\mathrm{C}_{1}$ and $\mathrm{C}_{6}$. Finally, the normal KIE at $\mathrm{C}_{3}$ and $\mathrm{C}_{4}$ of 2,5-diphenyl-1,5-hexadiene is roughly one eighth of the inverse KIE at $\mathrm{C}_{1}$ and $\mathrm{C}_{6}$. Thus the transition-

